

The 10th Industrial Fluid Properties Simulation Challenge

The Pressure-Viscosity Relation

p / MPa	η / mPa·s
0	0.640
25	0.844
50	1.101
100	1.71
150	2.54
250	5.31
350	10.67
400	15.0
500	30.9
600	62.9
700	126.9
800	264
900	558
1000	1187

←====5.13

$$\alpha^* = \left[\int_0^\infty \frac{\eta(p=0) dp}{\eta(p)} \right]^{-1}$$

$$\alpha^* \approx \left[\frac{\eta_0}{\alpha_N \eta_N} + \sum_{i=1}^N \frac{\eta_0}{\alpha_i} \frac{\eta_i - \eta_{i-1}}{\eta_i \eta_{i-1}} \right]^{-1} = 8.85 \text{ GPa}^{-1}$$

$$\alpha(p = 0.9 \text{ GPa}) = \left. \frac{d(\ln \eta)}{dp} \right|_{p=0.9 \text{ GPa}}$$

$$\alpha \left(p = \frac{p_i + p_{i-1}}{2} \right) \approx \frac{\ln(\eta_i / \eta_{i-1})}{(p_i - p_{i-1})}$$

$$\alpha(p = 0.9 \text{ GPa}) \approx 7.5 \text{ GPa}^{-1}$$

The 10th Industrial Fluid Properties Simulation Challenge

The Pressure-Viscosity Relation

Maximum total points = 100

p / MPa	Category	Tolerance	Full Points
0	Viscosity	4.9%	15
25	Viscosity	4.9%	2
50	Viscosity	4.8%	2
100	Viscosity	4.7%	3
150	Viscosity	4.7%	3
250	Viscosity	4.9%	3
400	Viscosity	5.5%	3
500	Viscosity	6.0%	3
600	Viscosity	6.4%	4
700	Viscosity	6.9%	4
800	Viscosity	7.5%	4
900	Viscosity	8.0%	6
1000	Viscosity	8.5%	8
	α^*	11.3%	20
	$\alpha(p=900)$	13.3%	20

film thickness

friction

Relative Error is defined as $\varepsilon = \frac{X_{MD}}{X_{exp}} - 1$ Full points are awarded for $|\varepsilon| < t$

The tolerance on viscosity is the greatest relative error expected in the experimental measurement if the error in viscosity, temperature and pressure are all equal to the estimated uncertainty. The tolerance on pressure-viscosity coefficient is simply based on error of 1 GPa^{-1} . The points awarded for each of the 15 categories is $F \times \text{Full Points}$.

If $|\varepsilon| < t$, then $E = 0$. Else if $\varepsilon > t$, then $E = \varepsilon - t$ and if $\varepsilon < -t$, then $E = \varepsilon + t$.

$$F = \frac{1}{\exp(sE)} \text{ where } s = 3.$$

The 10th Industrial Fluid Properties Simulation Challenge The Pressure-Viscosity Relation

